

6.2 Multiplying and Dividing Rational Expressions

Multiplying and dividing rational expressions is similar to multiplying and dividing rational numbers. We need to ensure we are identifying non-permissible values as we work our way through simplifying an expression.

Example: Simplify each expression. Identify all non-permissible values

a) $\left(\frac{4x^2}{3xy}\right)\left(\frac{y^2}{8x}\right)$ $x \neq 0, y \neq 0$

$$= \frac{4x^2y^2}{24x^2y}$$

$$= \frac{y}{6}, x \neq 0, y \neq 0$$

b) $\left(\frac{3x^2}{y^2}\right) \div \left(\frac{x}{y}\right)$ $y \neq 0$

$$= \frac{3x^2}{y^2} \cdot \frac{y}{x}, x \neq 0$$

$$= \frac{3x}{y}, x \neq 0, y \neq 0$$

Recall: To divide fractions we multiply by the reciprocal of the second fraction

Factor first

c) $\frac{x^2-x-12}{x^2-9} \times \frac{x^2-4x+3}{x^2-4x}$

$$= \frac{(x-4)(x+3)}{(x+3)(x-3)} \cdot \frac{(x-1)(x-3)}{x(x-4)}$$

$x \neq \pm 3, 0, 4$

$$= \frac{x-1}{x}, x \neq \pm 3, 0, 4$$

Remember that you CANNOT cancel the x s out here!!!

d) $\frac{x^2-9}{y^3-y} \times \frac{y^2-y}{x+3}$

$$= \frac{(x+3)(x-3)}{y(y^2-1)} \cdot \frac{y(y-1)}{(x+3)}$$

$$= \frac{(x+3)(x-3)y(y-1)}{y(y+1)(y-1)(x+3)}$$

$y \neq 0, \pm 1, x \neq -3$

$$= \frac{x-3}{y+1}, x \neq -3, y \neq \pm 1, 0$$

Factor by Decomposition

$$e) \frac{x^2 - 4}{x^2 - 4x} \div \frac{2x^2 - x - 6}{x^2 + x - 20}$$

	2x + 3	
x	2x ²	+ 3x
-2	- 4x	- 6

$$= \frac{(x+2)(x-2)}{x(x-4)} \div \frac{(2x+3)(x-2)}{(x+5)(x-4)}$$

$x \neq -5, 0, 4$

$$= \frac{(x+2)\cancel{(x-2)}}{x\cancel{(x-4)}} \cdot \frac{(x+5)\cancel{(x-4)}}{(2x+3)\cancel{(x-2)}}$$

$x \neq -3/2, 2$

$$= \frac{(x+2)(x+5)}{x(2x+3)}$$

$x \neq -5, -3/2, 0, 2, 4$

$$f) \frac{3x+12}{3x^2-5x-12} \div \frac{12}{3x+4} \cdot \frac{2x-6}{x+4}$$

	3x + 4	
x	3x ²	+ 4x
-3	- 9x	- 12

$$= \frac{3(x+4)}{(x-3)(3x+4)} \div \frac{12}{(3x+4)} \cdot \frac{2(x-3)}{(x+4)}$$

$x \neq -4, -4/3, 3$

$$= \frac{3\cancel{(x+4)}}{\cancel{(x-3)}\cancel{(3x+4)}} \cdot \frac{\cancel{(3x+4)}}{\rightarrow 12} \cdot \frac{\cancel{2(x-3)}}{\cancel{(x+4)}}$$

no new non-permissible values!

$$= \frac{6}{12}$$

$$= \frac{1}{2}, \quad x \neq -4, -4/3, 3$$