

Pre-Calculus 11

Chapter 7: Absolute Value and Reciprocal Functions

7.1 Absolute Value

Absolute value: For a real number, a , the absolute value is written as $|a|$.

Essentially, to take the absolute value of a number means to ask how far away it is from zero.

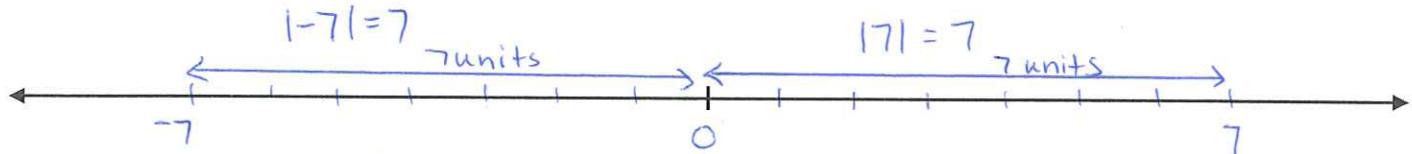
- The absolute value of a positive number is always positive.

$$|7|=7$$

- The absolute value of a negative number is always positive.

$$|-7|=7$$

- The absolute value of zero is zero. $|0|=0$



In general: $|n| = \begin{cases} n, & \text{if } n \geq 0 \\ -n, & \text{if } n < 0 \end{cases}$ ← this is called a piecewise function
think: $|5|=5$ and $|-5|=-(-5)=5$

Example: Evaluate each expression.

a) $|-12|$

$= 12$

b) $|-4| - |-3|$

$= 4 - 3$

$= 1$

c) $5 - 3|2 - 7|$ treat it like brackets.

$= 5 - 3|-5|$

$= 5 - 3(5)$

$= 5 - 15$

$= -10$

d) $|12(-3) + 5^2|$

$= |-36 + 25|$

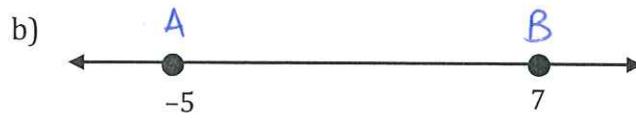
$= |-11|$

$= 11$

Example: Write two different absolute value expressions to represent the distance between points A and B.



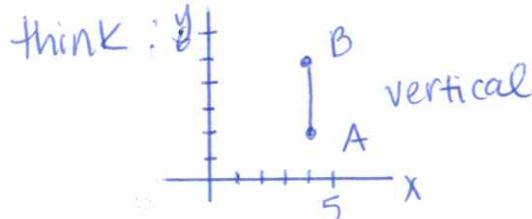
$$\begin{aligned} &|13-4| \quad \text{OR} \quad |4-13| \\ &= |9| \\ &= 9 \end{aligned}$$



$$\begin{aligned} &|7-(-5)| \quad \text{OR} \quad |-5-7| \\ &= |12| \\ &= 12 \end{aligned}$$

Example: Use absolute value symbols to write an expression for the length of each horizontal or vertical line segment.

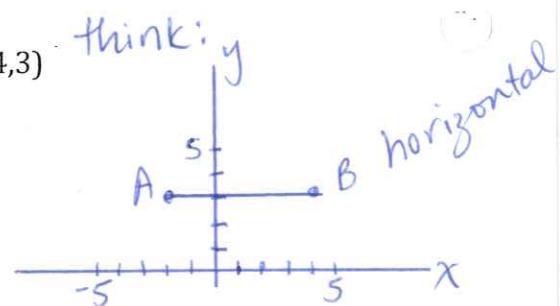
a) A(4,2) to B(4,5)



$$|5-2|=3$$

b) A(-2,3) and B(4,3)

$$\begin{aligned} & |-2-4| \\ & = 6 \end{aligned}$$

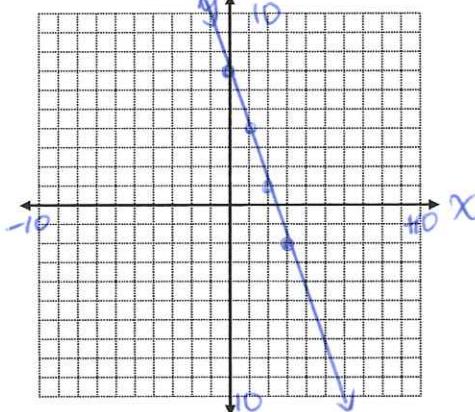


think: y

We will need to use our knowledge of graphing linear and quadratic functions in this unit.

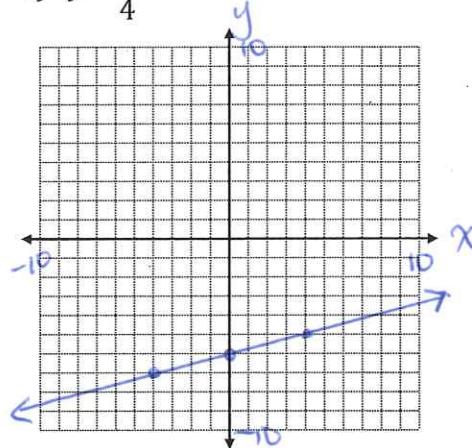
Example: Graph each function. Clearly label axes and scale.

a) $y = -3x + 7$



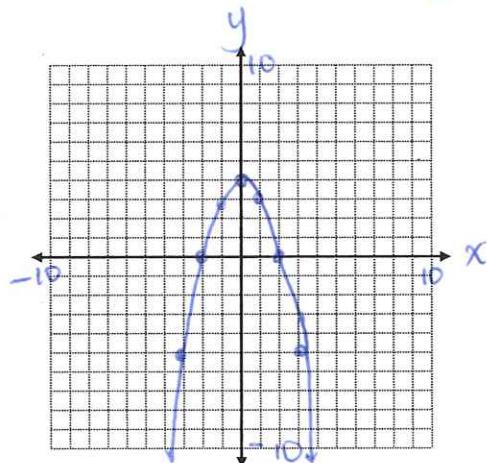
math 10

b) $y = \frac{1}{4}x - 6$



c) $y = -x^2 + 4$

earlier this year!



d) $y = (x-5)^2 + 1$

vertex: $(5, 1)$

