

7.5 Solving Linear Systems by Elimination
(addition/subtraction method)

Goal: To eliminate one variable by adding or subtracting the two equations of the linear system.

Example: Solve each of the following systems of equations using the elimination method.

a) $3x + y = 13$
 $x + y = 3$

$$\begin{array}{r} 3x + y = 13 \\ - (x + y = 3) \\ \hline 2x = 10 \\ \frac{2x}{2} = \frac{10}{2} \\ x = 5 \end{array}$$

Solution:
 $(5, -2)$

$$\begin{array}{r} x + y = 3 \\ 5 + y = 3 \\ y = -2 \end{array}$$

b) $2x + 3y = 18$
 $2x - 3y = -6$

$$\begin{array}{r} 2x + 3y = 18 \\ + (2x - 3y = -6) \\ \hline 4x = 12 \\ x = 3 \end{array}$$

$$\begin{array}{r} 2x - 3y = -6 \\ 2(3) - 3y = -6 \\ 6 - 3y = -6 \\ -3y = -12 \\ y = 4 \end{array}$$

Solution:
 $(3, 4)$

$$\begin{array}{r}
 \text{c) } \begin{cases} 3x + y = 18 \\ x + 2y = 11 \end{cases} \rightarrow \begin{array}{r} 3x + y = 18 \\ - 3x + 6y = 33 \\ \hline -5y = -15 \\ y = 3 \end{array}
 \end{array}$$

$$\begin{array}{r}
 3x + y = 18 \\
 3x + 3 = 18 \\
 3x = 15 \\
 x = 5
 \end{array}$$

Solution:
(5, 3)

$$\begin{array}{r}
 \text{d) } \begin{cases} 3x - 5y = 7 \\ 5x - 2y = -1 \end{cases} \begin{matrix} 2 \\ 5 \end{matrix} \rightarrow \begin{array}{r} 6x - 10y = 14 \\ - 25x - 10y = -5 \\ \hline -19x = 19 \\ x = -1 \end{array}
 \end{array}$$

$$\begin{array}{r}
 3x - 5y = 7 \\
 3(-1) - 5y = 7 \\
 -3 - 5y = 7 \\
 -5y = 10 \\
 y = -2
 \end{array}$$

Solution:
(-1, -2)

$$\text{e) } \begin{cases} \frac{3}{4}x - y = 2 \\ \frac{1}{8}x + \frac{1}{4}y = 2 \end{cases} \begin{matrix} 4 \\ 8 \end{matrix}$$

$$\begin{array}{r}
 \rightarrow 3x - 4y = 8 \rightarrow 3x - 4y = 8 \\
 3(x + 2y = 16) \rightarrow - 3x + 6y = 48 \\
 \hline -10y = -40 \\
 y = 4
 \end{array}$$

$$\begin{array}{r}
 3x - 4y = 8 \\
 3x - 4(4) = 8 \\
 3x - 16 = 8 \\
 \rightarrow 3x = 24 \\
 x = 8
 \end{array}$$

Solution
(8, 4)