Foundations and Pre-Calculus 10 Sequences and Series: Assignment 6

## **Sequences and Series Review**

- 1. Determine which of the following sequences are arithmetic. If the sequence is arithmetic, determine the common difference and the next 4 terms.
- a) 8, 11, 14, ... b) 2, 6, 18, ... c) 8, 4, 2, ... f) 1, 1, 2, 3, 5, ... f) 1, 1, 2, 3, 5, ...
- 2. Given the arithmetic sequence 10, 7, 4, ...
- a) Determine the 21<sup>st</sup> term. b) Which term is –77?
- 3. Find the missing terms in each arithmetic sequence.

a), 10, 16,,	b), 9,,, -3	c) 5,, 44
d) -3,,, 12	e) 3.4,,, -2,	f) 1.5,,, 0,

- 4. An arithmetic sequence has a 10th term of 18 and a 14th term of 30. Find the common difference and the first term.
- 5. Find the sum of the following arithmetic series.
- a) 5, 9, 13, ..., 101 b) 83, 80, 77, ..., 5
- 6. Find the sum of the following arithmetic series.
- a) The first 16 terms of 4, 11, 18 ... b) The first 10 terms of 19, 13, 7, ...
- 7. Find the sum of the first 100 odd numbers.
- 8. Jerry deposited \$20,000 on an investment that will give \$1,750 for every year that his money stays in the account. How much money will he have in his account by the end of year 8?
- 9. How many terms are in the arithmetic series  $3 + \dots + 59$  if the sum is 465?

- 10. In his piggy bank, Bingo dropped \$1.00 on May 1, \$1.75 on May 2, \$2.50 on May 3 and so on until the last day of May.
- a) How much did he drop in his piggy bank on May 19?
- b) What was his total deposit in his piggy bank for the month of May?
- 11. The sum of the first 7 terms of an arithmetic series is 63. The sum of the first 8 terms is 92. The common difference is 5. Determine the first 3 terms.
- 12. Determine the indicated term of each geometric sequence.

a) 1, 2, 4, ....*t*<sub>14</sub> b) 6, 1.2, 0.24, .... *t*<sub>7</sub>

13. Consider the geometric series:  $\frac{16}{9}$ ,  $-\frac{4}{3}$ , 1, ...

a) Write an expression for the general terms of this series.

- b) How many terms are there if the last term is  $-\frac{3888}{9216}$ ?
- 14. Insert two numbers between 26 and 702 so that the four numbers will form a geometric sequence.
- 15. A culture initially has 5000 bacteria and the number increases by 8% every hour.
- a) How many bacteria are present at the end of 5 hours?

b) Determine a formula for the number of bacteria present after n hours.

## Answers:

d) d=1.4; 1.7, 3.1, 4.5, 5.9 e) d=-4; 8, 4, 0, -4 1a) d=3; 17, 20, 23, 26 2a) -50, b)  $t_{30}$ 3a) 4, 10, 16, 22, 28 b) 13, 9, 5, 1, -3 c) 5, 18, 31, 44 d) -3, 0.75, 4.5, 8.25, 12 e) 3.4, 1.6, -0.2, -2, -3.8 f) 1.5, 1, 0.5, 0, -0.5 4) d=3; a=-9 5a) 1325 b) 1188 6a) 904 b) -80 10a) \$14.50 b) \$379.75 7) 10 000 8) \$34 000 9) 15 1 13a)  $t_n = \frac{16}{9} \left( -\frac{3}{4} \right)^{n-1}$  b)  $t_6$ 11) -6, -1, 4 12a) 8192 b) 0.000384 14) 78, 234 15a) about 7347 bacteria b)  $t_n = 5000(1.08)^n$